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# Low-energy charge transfer excitations in NiO

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**Abstract.** Comparative analysis of photoluminescence (PL) and photoluminescence excitation (PLE) spectra of NiO poly- and nanocrystals in the spectral range 2-5.5 eV reveals two PLE bands peaked near 3.7 and 4.6 eV with a dramatic rise in the low-temperature PLE spectral weight of the 3.7 eV PLE band in the nanocrystalline NiO as compared with its polycrystalline counterpart. In frames of a cluster model approach we assign the 3.7 eV PLE band to the low-energy bulk-forbidden p-d ( $t_{1g}(\pi)$ - $e_g$ ) charge transfer (CT) transition which becomes the allowed one in the nanocrystalline state while the 4.6 eV PLE band is related to a bulk allowed d-d ( $e_g$ - $e_g$ ) CT transition scarcely susceptible to the nanocrystallization. The PLE spectroscopy of the nanocrystalline materials appears to be a novel informative technique for inspection of different CT transitions.

#### 1. Introduction

Despite several decades of studies there is still no literature consensus on the detailed electronic structure of the prototype 3d oxide NiO, in particular, the character of the low-energy charge transfer excitations. NiO has long been viewed as a prototype "Mott insulator" [1] with a gap formed by intersite d-d charge transfer (CT) transitions, however, this view was later replaced by that of a "CT insulator" [2] with gap formed by p-d CT transitions. At present we have no comprehensive assignment of intensive spectral features in NiO to different p-d or d-d CT transitions. The main reason for this is that the absorption coefficient rises steeply above  $3.5\,\mathrm{eV}$  and reaches a giant value of  $10^6\,\mathrm{cm}^{-1}$  at and above  $4\,\mathrm{eV}$  [3] that complicates the detailed absorption and reflection measurements particularly near the fundamental edge. This difficulty can be avoided in part by making use of specific techniques such as electroreflectance measurements [4] or nonlinear absorption measurements [5] that are particularly effective for location of the forbidden transitions.

Main goal of our paper is to show with NiO as an example that the photoluminescence excitation (PLE) spectroscopy of the nanocrystalline materials appears to be a novel informative technique for inspection of different charge transfer transitions. Indeed, on the one hand, nanocrystalline state gives rise to a noticeable modification of the optical response of materials, in particular, due to an enhanced role of the surface induced local structural distortions resulting in a shift and splitting of the energy levels, and, mainly, in a liberalization of the

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selection rules. It means that optical response of nanocrystalline materials can reveal electronhole excitations unresolved in bulk spectra. On the other hand, the photoluminescence (PL) spectroscopy can give a profound insight into the electronic structure, electron-hole excitations and their relaxation in the lattice. As regards nanocrystalline NiO, its optical properties both in absorption and emission have been scarcely investigated. To the best of our knowledge the photoluminescence studies of nanocrystalline NiO are restricted by just two papers [6, 7]. Volkov et al. [6] have performed the steady-state absorption and time-resolved luminescence measurements for nanoclustered NiO samples with the particle size of 0.6 nm. The authors of Ref. [7] have presented certain controversial results of absorption and photoluminescence measurements for NiO nanocrystals with the particle size of 40 nm. However, in the both researches there is no inspection of the PL photoexcitation over the CT band, though such a study together with the comparative analysis of the poly- and nanocrystalline NiO PL and PLE spectra can be an instructive tool to elucidate the mechanism of the CT transitions and the spectral selectivity of the photoluminescence. These issues did motivate our studies of the PL and PLE spectra in nanocrystalline NiO samples as compared with polycrystalline samples.

#### 2. Experimental results

In order to make clear the effect of nanocrystallization the PL measurements were made both on conventional polycrystalline and nanocrystalline samples of NiO. As a starting material for polycrystalline NiO we have used the commercially available powder of NiO (99%; Prolabo) which has been pressed into pellets under pressure of about 0.125 GPa and placed into gold capsules. Quenching experiments at 7.7 GPa and 1000-1100 K have been performed using a toroid-type high-pressure apparatus. Detailes of experimental technique and calibration are described elsewhere [8]. Electron microscopy analysis shows the samples to be dense poreless oxide ceramics with rock salt cubic structure and grain size of about  $10-20 \,\mu\mathrm{m}$ . Nanocrystalline samples of NiO with a particle size of 25 nm were produced by the gas-condensation synthesis method [9] and annealed in air at a temperature of 350° C for an 24 hour. The samples for our measurements were produced by tablet pressing at a pressure of 0.5 GPa. The PL and PLE spectra were measured in the range (2-5.5) eV using two double DMP-4 prism monochromators (a reciprocal linear dispersion of 10 Å/mm near 5 eV), an R6358-10 (Hamamatsu) photomultiplier tube, and a photon-counting system [10, 11]. A deuterium DDS-400 lamp was used for excitation. The PLE spectra were normalized to the same number of photons incident on the sample using yellow phosphor, which has an energy-independent PL quantum yield in the energy range under investigation. The PL spectra are presented without any normalization to the spectral sensitivity of the optical section. Typical PL spectra of poly- and nanocrystalline NiO samples measured at room temperature and low temperature T = 90 K under excitation energies suggestive the CT band excitation  $(E_{exc} > E_g)$  are presented in upper and lower panels of Fig. 1, respectively. Such a broad luminescence band in the region 2-3.5 eV was observed in earlier PL measurements performed with UV excitation below and near optical gap [12, 6, 13]. The lowenergy excitation  $(E_{exc} \approx 2.4 \,\mathrm{eV})$  below the charge-transfer gap stimulates a photoemission in single-crystal NiO with two maxima, one at 1.5-1.6 eV and a larger one at 2.2-2.3 eV [14]. Green luminescence band with a maximum around 2.25 eV has been observed in nanoclustered NiO at  $E_{exc} \leq 2.95 \,\mathrm{eV}$  [6]. The observed emission bands in the visible and near infrared spectral ranges are usually attributed to  $Ni^{2+}$  intrasite, or crystal field d-d transitions. In particular, the main green luminescence band peaked near 2.3 eV is attributed to a Stokesshifted  ${}^{1}T_{2q}(D) \rightarrow {}^{3}A_{2q}(F)$  transition while the low-energy band peaked near 1.5 eV is related to  ${}^{1}E_{q}(D) \rightarrow {}^{3}A_{2q}(F)$  transition [14] (see Ref. [3] for the spectrum of the crystal field d-dtransitions). However, the photoluminescence spectra of bulk single crystals and ceramics of NiO under 3.81 eV photoexcitation [13] suggestive the band gap excitation have revealed in addition to the green band a more intensive broad violet PL band with a maximum around

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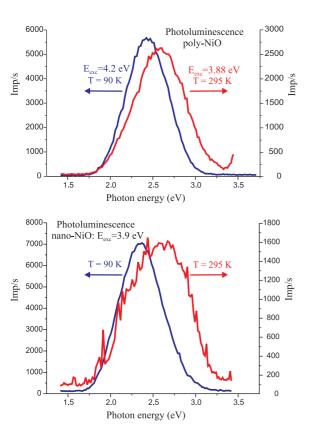


Figure 1. (Color online) Photoluminescence spectra of polycrystalline (upper panel) and nanocrystalline (lower panel) NiO samples at two temperatures and  $E_{exc} > E_q$ .

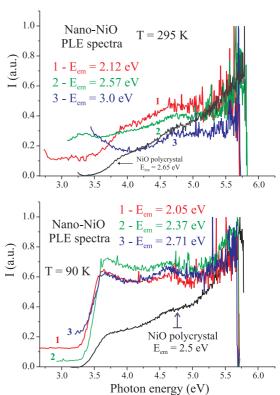


Figure 2. (Color online) The PLE spectra of nanocrystalline NiO at two temperatures  $(T=295\,\mathrm{K},\;\mathrm{upper\;panel},\;T=90\,\mathrm{K},\;\mathrm{lower\;panel})$  and different emission energies. For comparison in the both panels shown are the PLE spectra of polycrystalline NiO at corresponding temperatures.

 $3\,\mathrm{eV}$ . The band was related to a p-d charge transfer. Radiative recombination of carriers in powdered pellets of NiO under UV excitation with  $E_{exc}=4.43\,\mathrm{eV}$  (280 nm) higher than the CT gap consists at  $10\,\mathrm{K}$  of a broad intensive band peaked at  $2.8\,\mathrm{eV}$  with a shoulder centered at about  $3.2\,\mathrm{eV}$  [12]. At variance with Ref. [13] the PL emission bands observed in the work [12] were attributed to the crystal field d-d transitions. Fig. 1 clearly shows the blue shift of the PL band with increasing the temperature both for polycrystalline and nanocrystalline samples of NiO. Such a behavior was noticed in earlier measurements for polycrystalline samples of NiO [12]. Furthermore, the detailed temperature measurements [12] indicate that the broad PL spectra of NiO consist of several components with relative intensity dependent on the temperature and excitation energy.

Different kinetic properties, seemingly different temperature behavior [12] point to different relaxation channels governing the green and violet luminescence. Despite the PL spectra for nanocrystalline and polycrystalline NiO have similar lineshape, it is worth noting a clear red shift of the low-temperature PL spectra and a visible assymetry of the high-temperature PL spectra for nano-NiO.

Main results of our paper are related with the PLE spectral measurements in range 2-5.5 eV presented in Fig. 2. The polycrystalline NiO sample reveals a rather structureless PL excitation spectrum with a steep spectral weight rise from 3.3 towards 6 eV and scarcely marked

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weak features near 3.7 and 4.6 eV. The low-energy feature becomes more pronounced at low temperatures T = 90 K. The room temperature PLE spectra for nanocrystalline NiO corroborates the presence of at least the 4.6 eV feature while the obscure lower energy spectral behavior strongly depends on the emission energy. Just another lower energy spectral behavior in PLE spectra for nanocrystalline NiO is observed at low temperature T = 90 K (see lower panel in Fig. 2). Here we see a dramatic rise in the PLE spectral weight with a peak at excitation energy  $E_{exc} \approx 3.7 \,\mathrm{eV}$  that points to the energy  $E_g^{PLE} \approx 3.5 \,\mathrm{eV}$  as a specific PLE gap for the both polyand nanocrystalline NiO. Interestingly that the spectral weight and position of the 4.6 eV PLE feature seem to weakly alter in between poly- and nanocrystalline NiO samples. Thus, we are drawn to the conclusion that the 3.7 eV band can be most likely related with the bulk-forbidden CT transition which becomes the allowed one in the nanocrystalline state while the 4.6 eV PLE band is believed to be related with a bulk allowed CT transition scarcely susceptible to the nanocrystallization. Such an attribution is supported by several arguments:

- 1. Electroreflectance spectra for bulk NiO [4] which detect the dipole-forbidden CT transitions clearly point to a forbidden transition peaked near 3.7 eV missed in reflectance and absorption spectra [3, 15, 16].
- 2. At variance with the bulk NiO a clearly visible intensive peak near 3.6-3.7 eV has been observed in absorption spectra of NiO nanoparticles [6, 7, 17]. Its intensity points to the CT origin.
  - 3. Peak near 3.8 eV has been observed in nonlinear absorption spectra of NiO [5].
  - 4. Photoconductivity threshold in bulk NiO has been observed at 3.7 eV [18].
- 5. A rather strong CT band peaked at 4.5 eV is clearly visible in the absorption of thin NiO films [19], RIXS spectra [20, 21], the reflectance spectra (4.3 eV) [15], the nonlinear absorption spectra [5]. All this points to dipole-allowed CT transition.

Below we will address the microscopic origin of the CT transitions defining the PLE bands at 3.7 and  $4.6\,\mathrm{eV}$ .

### 3. Discussion

Despite the nature of radiative and nonradiative transitions in strongly correlated 3d oxides is far from full understanding some reliable semiquantitative predictions can be made in frames of a simple cluster approach (see, e.g. Refs. [22] and references therein). The method provides a clear physical picture of the complex electronic structure and the energy spectrum, as well as the possibility of a quantitative modelling. In a certain sense the cluster calculations might provide a better description of the overall electronic structure of insulating 3d oxides than the band structure calculations, mainly due to a better account for correlation effects. Starting with octahedral NiO<sub>6</sub> complex with the point symmetry group  $O_h$  we deal with five Ni 3d and eighteen oxygen O 2p atomic orbitals forming both hybrid Ni 3d-O 2p bonding and antibonding  $e_g$  and  $t_{2g}$  molecular orbitals (MO), and purely oxygen nonbonding  $a_{1g}(\sigma)$ ,  $t_{1g}(\pi)$ ,  $t_{1u}(\sigma)$ ,  $t_{1u}(\pi)$ ,  $t_{2u}(\pi)$  orbitals. Typically for the octahedral MeO<sub>6</sub> clusters the non-bonding  $t_{1g}(\pi)$  oxygen orbital has the highest energy and forms the first electron removal oxygen state while other nonbonding oxygen  $\pi$ -orbitals,  $t_{2u}(\pi)$ ,  $t_{1u}(\pi)$ , and  $\sigma$ -orbital  $t_{1u}(\sigma)$  have lower energy with the energy separation  $\sim 1 \, \text{eV}$  in between [22].

The p-d CT transitions in NiO<sub>6</sub><sup>10 $^{-}$ </sup> center are related with the transfer of the O 2p electron to the partially filled  $3de_g$ -subshell with formation on the Ni-site of the  $(t_{2g}^6e_g^3)$  configuration of nominal Ni<sup>+</sup> ion isoelectronic to the well-known Jahn-Teller Cu<sup>2+</sup> ion. Yet actually instead of a single p-d CT transition we arrive at a series of O  $2p\gamma \to Ni$   $3de_g$  CT transitions forming a complex p-d CT band. It should be noted that each single electron transition gives rise to two many-electron transitions. The band starts with the dipole-forbidden  $t_{1g}(\pi) \to e_g$ , or  ${}^3A_{2g} \to {}^3T_{1g}$ ,  ${}^3T_{2g}$  transitions, then includes two formally dipole-allowed so-called  $\pi \to \sigma$  p-d CT transitions, weak  $t_{2u}(\pi) \to e_g$ , and relatively strong  $t_{1u}(\pi) \to e_g$  CT transitions, respectively,

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each giving rise to  ${}^3A_{2g} \to {}^3T_{1u}, {}^3T_{2u}$  transitions. Finally main p-d CT band is ended by the strongest dipole-allowed  $\sigma \to \sigma \ t_{1u}(\sigma) \to e_g \ ({}^3A_{2g} \to {}^3T_{1u}, {}^3T_{2u})$  CT transition. Above estimates predict the separation between partial p-d bands to be  $\sim 1\,\mathrm{eV}$ . Thus, if the most intensive CT band with a maximum around 7 eV observed in RIXS spectra [20, 21] to attribute to the strongest dipole-allowed O  $2pt_{1u}(\sigma) \to Ni \ 3de_q \ CT$  transition then one should expect the low-energy p-d CT counterparts with maximum around 4, 5, and 6 eV respectively, which are related to dipoleforbidden  $t_{1g}(\pi) \to e_g$ , weak dipole-allowed  $t_{2u}(\pi) \to e_g$ , and relatively strong dipole-allowed  $t_{1u}(\pi) \to e_g$  CT transitions, respectively. It is worth noting that the  $\pi \to \sigma$  p-d CT  $t_{1u}(\pi) - e_g$ transition borrows a portion of intensity from the strongest dipole-allowed  $\sigma \to \sigma \ t_{1u}(\sigma) - e_q$ CT transition because the  $t_{1u}(\pi)$  and  $t_{1u}(\sigma)$  states of the same symmetry are partly hybridized due to p-p covalency and overlap. Interestingly that this assignment finds a strong support in the reflectance (4.9, 6.1, and 7.2 eV for allowed p-d CT transitions) [15] and, particularly, in electroreflectance spectra [15, 4] which detect dipole-forbidden transitions. Indeed, the spectra clearly point to a forbidden transition peaked near 3.7 eV (missed in reflectance spectra) which thus defines a p-d character of the optical CT gap and can be related with the on-set transition for the whole complex p-d CT band. It should be noted that a peak near  $3.8\,\mathrm{eV}$  has been observed in nonlinear absorption spectra of NiO [5]. A rather strong  $p(\pi)$ -d CT band peaked at 6.3 eV is clearly visible in the absorption spectra of MgO:Ni [16].

As a result of the p-d CT transition, a photo-generated electron localizes on a Ni<sup>2+</sup> ion forming Jahn-Teller 3d<sup>9</sup>, or Ni<sup>1+</sup> configuration, while a photo-generated hole can move more or less itinerantly in the O 2p valence band determining the hole-like photoconductivity [18]. The most effective channel of the recombinational relaxation for the spin-triplet p-d CT states  $t_{2g}^6 e_g^3 (\pi)$  ( $\gamma(\pi) = t_{1g}(\pi), t_{2u}(\pi), t_{1u}(\pi)$ ) implies the  $\pi \to \pi$  transfer  $t_{2g} \to \gamma(\pi)$  with formation of excited spin-triplet  ${}^3T_{1g}$  or  ${}^3T_{2g}$  states of the  $t_{2g}^5 e_g^3$  configuration of Ni<sup>2+</sup> ion followed by final relaxation to lowest singlet terms  ${}^1T_{2g}$  and  ${}^1E_g$  producing green and red luminescence, respectively. Obviously, this relaxation is strongly enhanced by any symmetry breaking effects lifting or weakening the selection rules. It means the three  $\pi \to \sigma p$ -d CT transitions  $t_{1g}(\pi) \to e_g$ ,  $t_{2u}(\pi) \to e_g$ , and  $t_{1u}(\pi) \to e_g$  are expected to effectively stimulate the green luminescence due to large effective mass of  $\pi$ -oxygen holes and a well-localized and long-lived character of the p-d excitation. On the other hand, the most intensive  $\sigma \to \sigma p$ -d CT transition  $t_{1g}(\sigma) \to e_g$  appears to be significantly less effective due to small effective mass of the  $\sigma$ -oxygen holes and relatively short lifetime of the respective unstable p-d CT state.

Along with the p-d CT transitions an important contribution to the optical response of strongly correlated 3d oxides can be related with strong d-d CT, or Mott transitions [22]. In NiO one expects a strong d-d CT transition related with the  $\sigma$ - $\sigma$ -type  $e_g$ - $e_g$  charge transfer  $t_{2g}^6 e_g^2 + t_{2g}^6 e_g^3 + t_{2g}^6 e_g^3 + t_{2g}^6 e_g^4$  between nnn Ni sites with the creation of electron [NiO<sub>6</sub>]<sup>11-</sup> and hole [NiO<sub>6</sub>]<sup>9-</sup> centers (electron-hole dimer), or nominally Ni<sup>+</sup> and Ni<sup>3+</sup> ions. This unique anti-Jahn-Teller transition  $^3A_{2g} + ^3A_{2g} \rightarrow ^2E_g + ^2E_g$  creates a d-d CT exciton self-trapped in the lattice due to electron-hole attraction and strong "double" Jahn-Teller effect for the both electron and hole centers.

Strong dipole-allowed Franck-Condon  $d(e_g)$ - $d(e_g)$  CT transition in NiO manifests itself as a strong spectral feature near  $4.5\,\mathrm{eV}$  clearly visible in the absorption of thin NiO films [19], the RIXS spectra [20, 21], the reflectance spectra  $(4.3\,\mathrm{eV})$  [15], the nonlinear absorption spectra  $(4.1\text{-}4.3\text{-}4.5\,\mathrm{eV})$  [5]. Such a strong absorption near  $4\,\mathrm{eV}$  is beyond the predictions of the p-d CT model and indeed is lacking in absorption spectra of MgO:Ni [16]. Accordingly, the CT gap in NiO is believed to be formed by a superposition of the electro-dipole forbidden p-d  $(t_{1g}(\pi) \to e_g)$  and allowed  $d(e_g)$ - $d(e_g)$  CT transitions with close energies that is NiO is close to the intermediate regime of the Zaanen-Sawatzky-Allen scheme. Thus we see that simple cluster model unambiguously points to the low-energy bulk-forbidden p-d  $(t_{1g}(\pi) \to e_g)$  and allowed  $d(e_g)$ - $d(e_g)$  CT transitions to be transitions responsible for the 3.7 and 4.6 eV bands revealed

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by the PLE spectroscopy of nanocrystalline NiO.

#### 4. Conclusion

In summary, we have measured the photoluminescence and photoluminescence excitation spectra of NiO poly- and nanocrystals in the spectral range 2-5.5 eV. The PL spectra for both types of samples have a very similar spectral shape with broad emission bands centered at about 2.5 eV. The PLE spectra reveal two PLE bands peaked near 3.7 and 4.6 eV with a dramatic rise in the low-temperature PLE spectral weight of the 3.7 eV PLE band in the nanocrystalline NiO as compared with its polycrystalline counterpart. We have performed a cluster model analysis of the CT transitions and assigned the 3.7 eV PLE band to the low-energy bulk-forbidden p-d ( $t_{1g}(\pi)$ - $e_g$ ) CT transition which becomes the allowed one in the nanocrystalline state while the 4.6 eV PLE band is related to the bulk allowed d-d ( $e_g$ - $e_g$ ) CT transition scarcely susceptible to the nanocrystallization. For the first time we succeded in distinct separating the contributions of the low-energy  $p(\pi)$ -d and d-d CT transitions to the fundamental absorption of NiO and show that NiO is close to the intermediate regime of the Zaanen-Sawatzky-Allen scheme. Thus, the PLE spectroscopy of the nanocrystalline materials is shown to be a novel informative technique for inspection of different CT transitions.

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