

The formation of Ti–O tetrahedra and band gap reduction in SiO₂ via pulsed ion implantation

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Titanium ions are implanted into amorphous SiO₂ at two different fluences using pulsed ion implantation, and the resulting samples are annealed. Bulk sensitive soft X-ray absorption spectroscopy of the Ti $L_{2,3}$ edge reveal strikingly different spectra for the two fluences. Spectral simulations using multiplet crystal field theory show clearly that for low fluence the Ti ions have a local octahedral coordination, while at higher fluence the formation of Ti⁴⁺–O tetrahedra dominates. Using O *K*-edge X-ray absorption and emission, the effect of the Ti states on the valence and conduction bands of the host SiO₂ is revealed. With the introduction of Ti tetrahedra, the band gap reduces from about 8 eV to just over 4 eV, due entirely to the Ti 3*d* conduction band states. These results demonstrate the possibility to obtain Ti–O tetrahedra in silica by Ti ion implantation and a suitable thermal treatment, clarify the mechanism of band gap reduction with Ti doping in SiO₂, and demonstrate the sensitivity of *L*-edge X-ray absorption with a multiplet crystal field theory analysis to the Ti coordination of novel materials. © 2013 American Institute of *Physics*. [http://dx.doi.org/10.1063/1.4795262]

I. INTRODUCTION

In recent years, the incorporation of 3*d* transition metals into semiconductors like ZnO and dielectrics like SiO₂ has been the topic of a vast number studies. Such materials show promise for a variety of technological applications based on the properties induced by the metal atoms. In some cases, the homogenous doping of transition metals into semiconductors leads to bulk ferromagnetic behavior, rendering the resulting material a dilute magnetic semiconductor¹ useful for spintronics² applications. Alternatively, using ion beam synthesis, the formation of metallic or metal-oxide embedded nanoparticles can be achieved.^{3,4} Dielectrics with embedded nanoparticles exhibit many useful properties such as nonlinear optical behavior, superparamagnetism, intense photoluminescence, and altered band structures.^{5,6}

The incorporation of Ti ions into SiO_2 (SiO₂:Ti) is an exciting topic because of the electronic properties of the constituents. The combination of the abundant Ti 3*d* conduction band states (due to the formally empty 3*d* shell of Ti⁴⁺) and the very wide band gap of SiO₂ implies a situation for strong electronic structure modification upon doping. Several synthesis techniques have been employed to study SiO₂:Ti in the past, including flame hydrolysis,⁷ the sol-gel method,^{8–11} chemical reduction,¹² and ion implantation.^{13–17} For certain Ti concentrations using flame hydrolysis or sol-gel, tetrahedral Ti⁴⁺ coordination has been found.^{7–9,11} However, using the ion implantation technique, only indirect evidence using

UV absorption has been found for T_d coordination¹⁴ so far. Other ion implantation studies revealed metallic Ti (Ref. 15) and Ti-composite nanoclusters.^{13,16,17}

The strong electronic structure modifications expected for SiO₂:Ti as alluded to above have also been only indirectly studied. A reduced band gap of 4 eV was found using optical absorption⁷ (compared to the pure SiO₂ gap of 8-9 eV). However, the individual valence and conduction bands have yet to be probed in the same experiment to show the mechanism behind this gap reduction. A full understanding of this process could yield a method to tailor the band gap through Ti doping.

In the current work we study the implantation of Ti ions into amorphous, bulk SiO2 using periodically pulsed ion implantation followed by thermal annealing. A combination of soft X-ray absorption (XAS) and X-ray emission spectroscopy (XES) is used to directly study the coordination of the Ti ions and the effects of implantation on the bulk electronic structure. Using Ti L-edge XAS and multiplet crystal field theory, we show that low fluences lead to octahedrally coordinated Ti while higher fluence promotes the formation of Ti-O tetrahedra. Oxygen K-edge XAS and XES reveal the hybridization of the Ti 3d and O 2p states for the Ti-O tetrahedra and show that the band gap narrowing is almost entirely a consequence of the Ti 3d states lowering the conduction band minimum. Our results demonstrate the utility of $L_{2,3}$ XAS for characterizing the Ti coordination in novel materials, demonstrate necessary parameters for producing Ti-O tetrahedra using ion implantation, and reveal the mechanism behind the band gap reduction in SiO₂:Ti.

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II. MATERIALS AND METHODS

The amorphous SiO₂ (*a*-SiO₂) samples used as targets for this study were 99.9% purity, plane-parallel glass plates measuring $1 \times 1 \text{ cm}^2$ with surfaces of optical quality and thicknesses of ~0.7 mm. Samples were irradiated with Ti⁺ ions using a pulsed source with an ion beam current density of ~2-7 mA/cm², implantation energy of 30 keV, and a pulse duration of 400 μ s. Ion fluences of $1 \times 10^{15} \text{ cm}^{-2}$ and $5 \times 10^{16} \text{ cm}^{-2}$ were used for two separate samples. During implantation the sample temperature was kept at 250 °C. After implantation the samples were annealed in air at 1000 °C for 1 h. A high-purity *a*-SiO₂ sample was also left unirradiated for use as a reference material.

An additional reference sample consisting of a $TiO_2:SiO_2$ mixture with 8% TiO_2 by weight was synthesized via melting 99.9% purity TiO_2 and SiO_2 in a corundum crucible. This stoichiometry corresponds atomic percentages of 2.0% Ti, 31.3% Si, and 66.7% O, or $(Si_{0.94}Ti_{0.06})O_2$. The sample was melted under normal atmosphere at 2000 °C for 3 h and then slowly cooled. All samples under study and references were prepared in the Ural Federal University (Yekaterinburg, Russia) using methods developed there.¹⁸

The depth dependence of the Ti ion concentration was calculated using the SRIM program.¹⁹ Simulations were performed using the same materials and implantation parameters implemented in experiment. The implantation of a total number of 10⁵ ions was simulated in order to obtain an adequately converged profile. Note that SRIM does not consider dynamic changes in the host material during the implantation process, so there is no fluence dependence in the profile shape.

Soft XES were measured using Beamline 8.01 of the Advanced Light Source (ALS) at Lawrence Berkeley National Laboratory.²⁰ The beamline uses a Rowland circle type diffraction grating spectrometer with a 90° scattering angle, and the incident radiation is plane-polarized within the horizontal scattering plane. Soft XAS were measured using the spherical grating monochromator (SGM) beamline of the Canadian Light Source (CLS) at the University of Saskatchewan.²¹ To ensure the entire implantation region was probed, spectra were collected using the bulk sensitive total fluorescence yield detection scheme, again with horizontal plane-polarized incident radiation. Note that for the $L_{2,3}$ edges of transition metal systems often the fluorescence yield is not a true measure of the XAS since the $3d \rightarrow 2p$ decay strengths can vary strongly for different XAS final states.²² However, for Ti⁴⁺ the 3s fluorescence channel is about as equally strong as the 3d, significantly suppressing the deviations from XAS.

To analyze the Ti $L_{2,3}$ XAS spectra, multiplet crystal field theory (MCFT) simulations were performed.²³ The simulations include full multiplet effects, as well as crystal field perturbations from neighbouring atoms. The calculated spectra were convolved with Lorentzian and Gaussian lineshapes to account for lifetime and experimental broadening, respectively.

III. RESULTS

Figure 1 shows the simulated concentration profile of Ti implanted in SiO_2 using the parameters implemented in our



FIG. 1. Ti concentration as a function of depth for the implanted samples. The left axis shows concentration for the 5×10^{16} cm⁻² fluence used in experiment, while the right axis is scaled for the 1×10^{15} cm⁻² fluence. Lines are shown to indicate the projected range (R_p), the standard deviation of the projected range (σ_{R_p}), and the average and maximum concentrations (η_{ave} and η_{max}).

experiment. From the simulation we find a projected range of $R_p = 31.8$ nm with a standard deviation (or straggle) of $\sigma_{R_n} = 11.8$ nm. Within the SRIM approach, there is no dependence of the profile shape on fluence, but different fluences will obviously lead to different concentrations. Thus, on the left axis of Figure 1 we give the Ti concentration considering an implantation fluence of 5×10^{16} cm⁻² while the right axis gives the concentration simulated for a fluence of 1×10^{15} cm⁻². The horizontal lines of the figure indicate the maximum Ti concentration (η_{max} , determined from the peak of a Gaussian lineshape fit to the profile) and the average Ti concentration (η_{ave}). For the higher fluence we find η_{max} = 19.5 at. % and η_{ave} = 6.9 at. % while for the lower fluence we find values of 0.39% and 0.14%, respectively. Thus the two fluences give average concentrations above and below the Ti concentration of the SiO₂:TiO₂ reference sample (2.0 at. %, as described earlier).

Figure 2 shows the experimental Ti $L_{2,3}$ XAS spectra for the implanted and reference samples. These spectra arise from the resonant excitation of Ti 2p electrons into bands of largely 3d character and are consequently very sensitive to the Ti oxidation state and coordination geometry. Immediately evident from Figure 2 is that there are striking differences between the spectra for the implanted samples prepared with different fluences. The spectrum for the higher fluence $(5 \times 10^{16} \text{ cm}^{-2})$ sample is very similar to that of the SiO₂:TiO₂ reference sample while the lower fluence $(1 \times 10^{15} \text{ cm}^{-2})$ sample exhibits different peak intensities and splittings. A spectrum recorded from rutile TiO₂ is shown in Figure 2 for reference. The spectrum looks very different from the other spectra, but as we shall show the characteristic lineshape from each sample is due to the local bonding symmetry. The different lineshapes are not due to a changing oxidation state; all samples are 4+. A look at the vastly different multiplet structure of a d^1 Ti³⁺ ion confirms this.²⁴

Transition metal $L_{2,3}$ XAS spectra of oxides and related materials are generally well understood^{23,25} and are well described by MCFT. For the Ti⁴⁺ cases shown here, the spectra can be roughly divided into two slightly overlapping



FIG. 2. Titanium $L_{2,3}$ -edge X-ray absorption spectra for implanted and reference samples. The spectra have been offset vertically for clarity.

(and interfering) regions which are split apart by the 2p spin orbit coupling: the L_3 region below ~461 eV and the L_2 region above this point. Within each of these regions, peaks are split apart generally by local crystal field effects. For TiO₂, for example, the L_2 and L_3 regions are split into roughly two peaks each, which correspond approximately to the e_g levels (at higher energies) and t_{2g} levels (at lower energies), due to the O_h coordination of the Ti ions. Note that there are other minor peaks present due to multiplet effects and that the e_g peaks exhibit a small splitting due partially to symmetry distortion and partially due to long-range effects.^{23,26}

Since the multiplet structures of these systems are welldescribed by MCFT, simulations were performed to determine the origin of the differences between the samples. The simulation results are shown in Figure 3, along with the corresponding experimental spectra. First considering the higher fluence case, we see excellent agreement is obtained with a calculation of a Ti⁴⁺ ion in tetrahedral (T_d) symmetry, using a 10 Dq value of $-0.90 \,\text{eV}$. This 10 Dq value is the energy splitting of the e and t_2 orbitals induced by bonding with neighboring atoms that distort the Ti 3d atomic orbitals from spherical symmetry. The negative sign indicates a tetrahedral T_d rather than octahedral O_h symmetry. This tetrahedral coordination of the Ti ions indicates they have been incorporated into Si sites of the SiO₂, and the spectra show a similar shape to experimental spectra of T_d Ti⁴⁺ in Ba₂TiO₄.²⁷ For the lower fluence case, however, the spectrum is best fit with a field of O_h symmetry (all parameters are shown in Table I). Here, a splitting of 1.75 eV was used, which is similar in magnitude compared to splittings found for other Ti^{4+} O_h systems such as FeTiO₃.²⁸ However, an additional Gaussian-like broadening is present in the experimental spectrum. To best reproduce the experimental data, an additional value of 0.25 eV was added to the FWHM of the Gaussian convolved with the simulated



FIG. 3. Titanium $L_{2,3}$ -edge X-ray absorption spectra for implanted and reference samples, along with calculated spectra of Ti⁴⁺ in T_d and O_h symmetries. The spectra have been offset vertically for clarity. The dotted spectrum is the result of subtracting 50% of the normalized 5×10^{16} cm⁻² spectrum from the normalized 1×10^{15} cm⁻² spectrum.

spectrum, compared to that of the T_d simulation (the same Lorentzian lifetime broadening was applied in each case). This additional broadening suggests that in this case the Ti ions are possibly located in interstitial regions of the SiO₂, where varying crystal field effects at different sites with varying geometries would broaden the spectrum. Finally, we note that the evident splitting of the peak at 459.4 eV for the 1 $\times 10^{15}$ cm⁻² sample indicates there are some T_d -coordinated Ti ions in this sample as well. A subtraction of a 50% fraction of the normalized higher fluence spectrum from the normalized lower fluence spectrum yields the dotted curve overlaid with the lower fluence spectrum. While this analysis is not meant to be quantitative, it does remove the lower half of the most intense peak and improves the agreement with the calculation, strongly suggesting that there are some T_d coordinated Ti ions present in the lower fluence sample.

Figure 4 displays the oxygen *K*-edge XAS and XES for the reference a-SiO₂ and the Ti-containing samples. Using these spectra, one can investigate the oxygen 2p-projected conduction and valence bands, respectively. Focusing on the XES first, we see minimal changes in the shape of the spectra for the various samples shown. As clarified in the inset, the spectra only gradually gain a small amount of spectral weight

TABLE I. Parameters used for the multiplet crystal field theory calculations. κ are rescaling factors for the intra-atomic Slater integrals, given as fractions of the Hartree Fock values.

Ion	Symmetry	10 <i>Dq</i> (eV)	κ
Ti ⁴⁺ Ti ⁴⁺	$O_h \ T_d$	$1.75 \\ -0.90$	0.75 0.65

on the low energy side of the main peak as the Ti content is increased. More significant changes are evident in the XAS, however, as prominent features are introduced in the pre-edge region from 531-535 eV as Ti is added to the samples. Stronger changes in the XAS compared to XES are expected, as the formally empty 3*d* shell of the Ti⁴⁺ ions means there are no occupied *d* states to contribute to the XES whereas there are ample empty states to contribute to the XAS.

The conduction band minimum (CB_{min}) and valence band maximum (VB_{max}) can be extracted from the XAS and XES using the second derivative technique,²⁹ and from these values the electronic band gap can be estimated. The second derivatives of the SiO₂ and SiO₂:TiO₂ spectra are shown at the bottom of Figure 4. It is found that both samples share a common VB_{max} , marked at point *a*, whereas the SiO₂:TiO₂ has a much lower conduction band minimum (point b) than pure SiO_2 (point c). Computing the differences between the maxima and minima yields estimated band gaps of $8.0 \pm 0.3 \text{ eV}$ for SiO₂ and $4.1 \pm 0.3 \text{ eV}$ for SiO₂:TiO₂. Within experimental error, the 5×10^{16} cm⁻² sample has the same CB_{min} and VB_{max} as SiO₂:TiO₂ but is not shown for clarity. These results agree with an earlier optical study which found a gap of 4 eV for SiO₂:Ti synthesized using flame hydrolysis.' However, here we can show that this reduction from the pure SiO₂ gap is due entirely to changes in the conduction band minimum energy.

IV. DISCUSSION

The Ti L edge results show very different relative amounts of T_d Ti coordination for the two samples. Two possible explanations for this can be considered. First, the T_d



FIG. 4. Oxygen *K*-edge X-ray absorption (right) and emission (left) spectra for implanted and reference samples. The XAS spectra have been offset vertically for clarity. For two of the samples, the second derivatives of the spectra are shown below and the common valence band maximum energy *a* and the conduction band minimum energies (*b* for SiO₂:TiO₂, *c* for SiO₂) are marked with vertical dotted lines.

coordination may be part of a stable phase of material where a certain ratio of Si and Ti is present. When too little Ti is present, it might not be energetically favorable to form Ti-O tetrahedra, and the Ti remains as interstitials. A second explanation is that with higher fluence, more damage to the host SiO₂ occurs during implantation. The higher degree of damage might allow for more incorporation of Ti into T_d sites. A preference to either explanation does not seem evident from the present results, but future experiments could be tailored to study this. Moreover, the specific changes induced by annealing could also be studied in future work since previous studies have found clusters of amorphous silicides¹³ and highly conductive metallic Ti layers¹⁵ in non-annealed samples synthesized with only slightly higher fluences than those used here. The application of L-edge XAS would provide a very useful study of the effects of the annealing process.

The oxygen edge results show the Ti induces a large effect on the SiO₂ band gap, reducing it to a range that is almost useful for electronic applications. The edge onset region of the O K XAS is generally very sensitive to transition metal 3d and oxygen 2p hybridization whereas the higher energy features are more sensitive to sp hybridization.³⁰ The 3d-sensitive region near the edge is often split into two peaks, and the degree of splitting is related to the local crystal field splitting. For TiO₂ this splitting is very prominent, as shown in the XAS spectrum in Figure 4 (in the region from 530 to 535 eV). For the SiO₂:TiO₂ and 5×10^{16} cm⁻² samples, however, this splitting is reduced, in agreement with the weaker T_d crystal field splitting found from the Ti L-edge XAS analysis. As clarified in the right hand inset of Figure 4, the lower fluence sample yields a spectrum very similar to the pure SiO₂ reference—both show a small bump at \sim 531.5 eV (likely due to defect states in the SiO₂), the two-peaked Ti structure is not evident, and there is only a somewhat constant increase in spectral weight for the lower fluence spectrum compared to SiO₂. The similarity of these spectra is perhaps not surprising, for a few reasons. First, there are \sim 50 times fewer Ti atoms in the 1×10^{15} cm⁻² sample compared to the 5×10^{16} cm⁻² sample so the Ti 3d character is expected to be very weak. Second, if the Ti atoms in the lower fluence sample are located primarily in interstitial regions as suggested earlier, the covalent interaction between the Ti and O atoms will be reduced, compared to the case where they are located in well defined tetrahedra. Third, the extra broadening that smeared the features of the Ti L edge XAS for the lower fluence sample would also affect the presence of the two-peaked structure in the O K XAS spectrum of this sample. Thus, the lack of distinct Ti 3d features in the 530–535 eV region is reasonable. Finally, we note that while the empty d shell for Ti leads to strong conduction band changes, the fuller d shells for elements like Ni and Cu should lead to useful changes in the valence band properties. By combining Ti implantation with Ni or Cu, one could then tailor both the valence and conduction bands, enabling further control over the band gap.

V. CONCLUSIONS

To conclude, we have studied Ti ion implanted SiO_2 samples and reference materials using soft XAS and XES.

The sensitivity of the Ti $L_{2,3}$ XAS to the Ti coordination was demonstrated, and it was shown that octahedral Ti coordination (possibly in interstitial regions) can be obtained by lowering the implantation fluence, while for high fluence the Ti showed tetrahedral coordination. Oxygen K-edge XAS spectra were used to probe the hybridization of the Ti 3d and O 2p states in the conduction band. Strong hybridization was observed for the high fluence and reference samples whereas the low fluence sample showed minimal interaction. From the oxygen XAS and XES the band gaps were extracted, yielding $8.0 \pm 0.3 \text{ eV}$ for SiO₂ and $4.1 \pm 0.3 \text{ eV}$ for a sample implanted with 5×10^{16} cm⁻² ions (and for a SiO₂:TiO₂ reference sample). These results demonstrate a change in Ti coordination with a change in fluence and the same postimplantation annealing, reveal the mechanism behind band gap reduction in SiO₂:Ti materials, and show the applicability of L-edge XAS with a multiplet crystal field theory interpretation for studying Ti coordination in novel materials.

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